

For each function, state the amplitude, if there is a reflection, the phase shift and the vertical shift. Write "none" for transformations that do not exist.

Then graph the function.

Step #1: Start by graphing the parent function $y = \sin \theta$ if there is no period change (b).

If there is a period change, find the new intervals first, then graph the parent graph as usual.

Step #2: Write the transformations IN THE ORDER IN WHICH THEY OCCUR

Step #3: Graph each transformation – one at a time, use more than one color!!!

Step #4: Label your final graph.

1. $y = \frac{2}{3} \sin(x)$

Period: _____

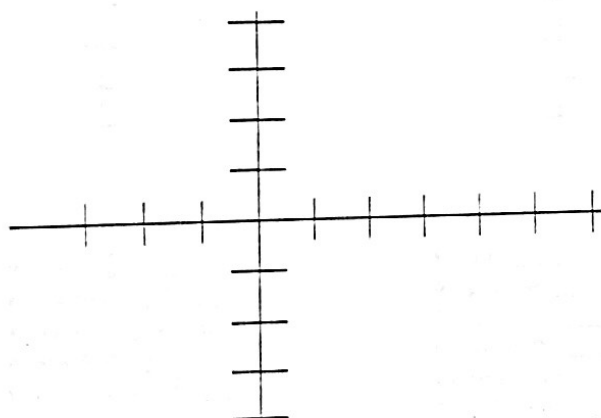
Amplitude: _____

Reflection: _____

Phase Shift: _____

Vertical Shift: _____

Transformations: _____



2. $y = 4 \sin(\pi x)$

Period: 2

Amplitude: 4

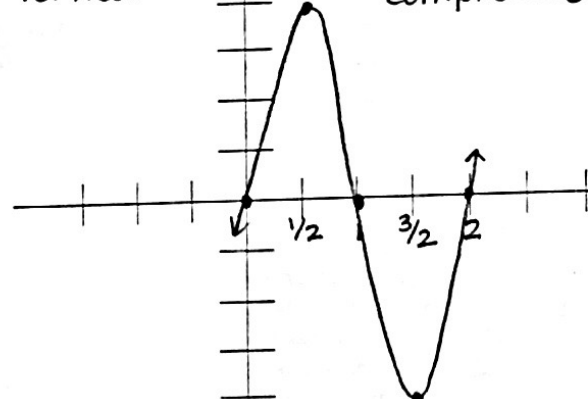
Reflection: none

Phase Shift: none

Vertical Shift: none

Transformations: _____

vertical stretch; horizontal compression



3. $y = 2 \sin \frac{1}{2} x$

Period: _____

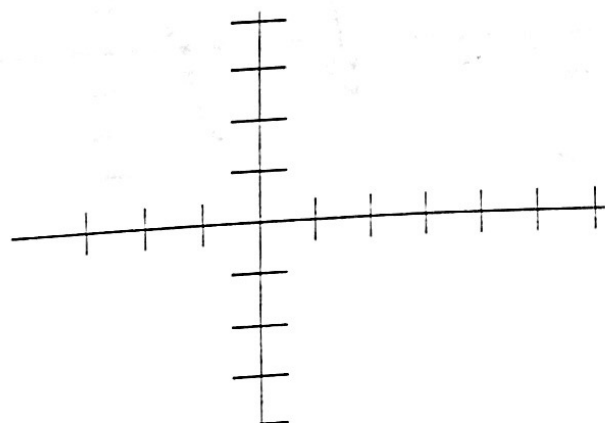
Amplitude: _____

Reflection: _____

Phase Shift: _____

Vertical Shift: _____

Transformations: _____



4. $y = \sin(x) + 3$

Period: 2π

Amplitude: 1

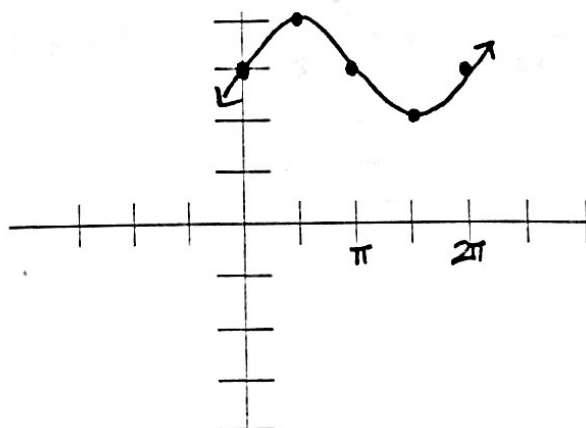
Reflection: none

Phase Shift: none

Vertical Shift: up 3

Transformations: _____

vertical translation up 3 units



5. $y = \sin(\frac{1}{2}x) - 4$

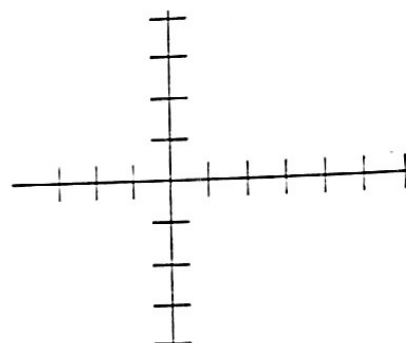
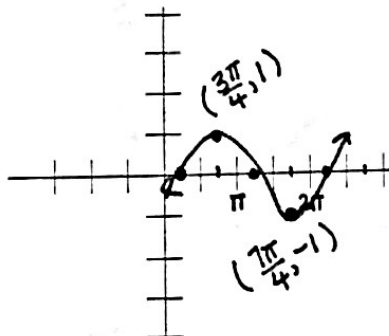
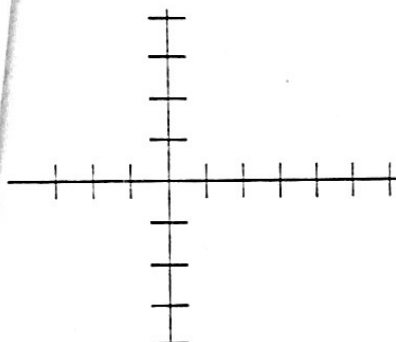
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____

6. $y = \sin(x - \frac{\pi}{4})$

Period: 2π
 Amplitude: 1
 Reflection: None
 Phase Shift: right $\pi/4$
 Vertical Shift: none
 Transformations: horizontal translation right $\pi/4$ units

7. $y = -\sin(\frac{1}{2}x + 3)$

Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



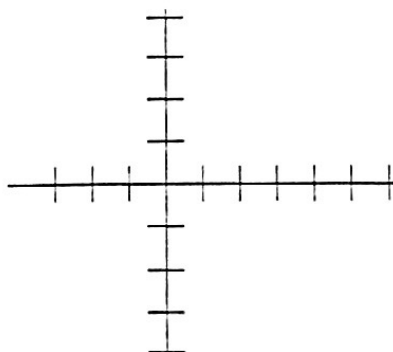
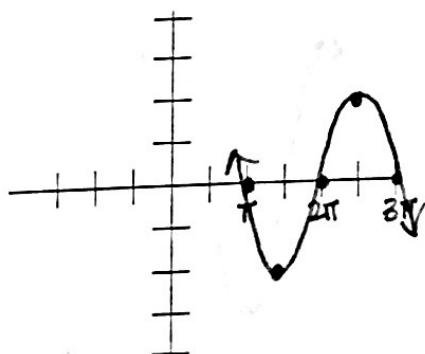
8. $y = -2\sin(x - \pi)$

Period: 2π
 Amplitude: 2
 Reflection: over x-axis
 Phase Shift: Right π
 Vertical Shift: None
 Transformations: _____

Reflect over x-axis
 vertical stretch: vert
 horizontal translation
 right π units

9. $y = 4\sin(x - \frac{3\pi}{2})$

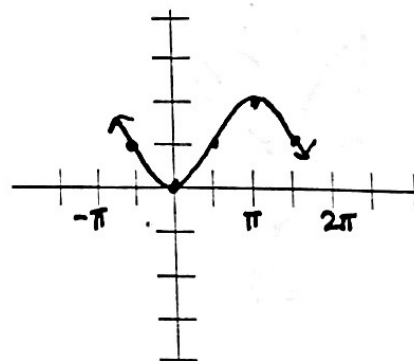
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



10. $y = -\sin(x + \frac{\pi}{2}) + 1$

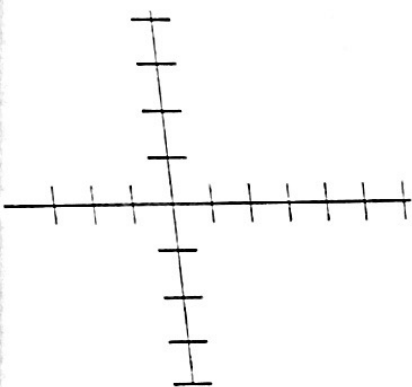
Period: 2π
 Amplitude: 1
 Reflection: over
 Phase Shift: left $\pi/2$
 Vertical Shift: up 1
 Transformations: _____

Reflection; horizontal
 shift left $\pi/2$ units,
 vertical shift up 1
 unit.



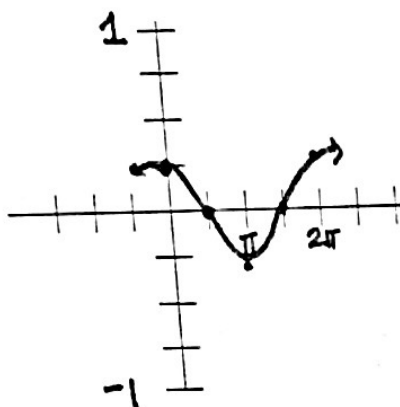
1. $y = 3 \sin(x + \pi) - 2$

Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



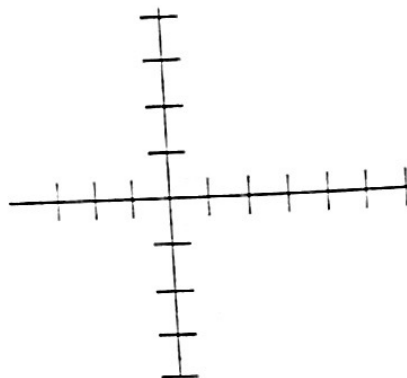
12. $y = \frac{1}{4} \cos x$

Period: 2π
 Amplitude: $1/4$
 Reflection: None
 Phase Shift: None
 Vertical Shift: None
 Transformations: Vertical shrink



13. $y = \frac{-2}{5} \cos x$

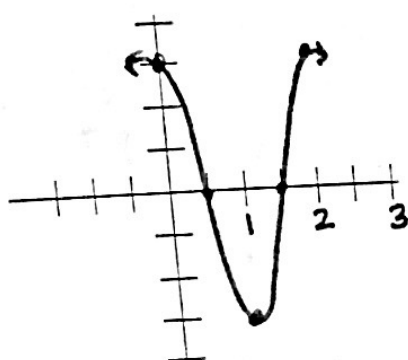
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



14. $y = 3 \cos \pi x$

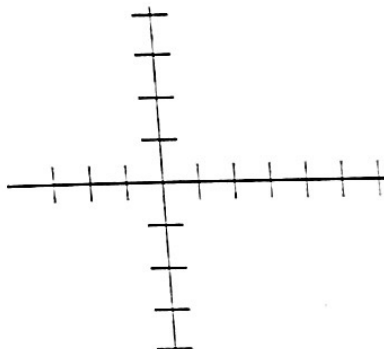
Period: 2
 Amplitude: 3
 Reflection: None
 Phase Shift: None
 Vertical Shift: None
 Transformations: _____

Vertical stretch by a factor of 3. Horizontal compression.



15. $y = \cos x - 5$

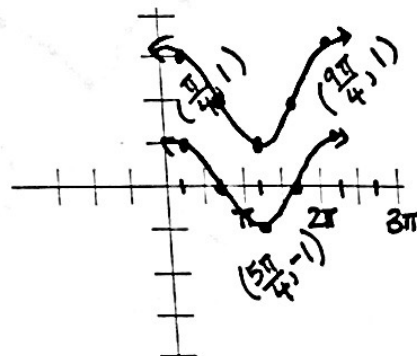
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



16. $y = \cos(x - \frac{\pi}{4}) + 2$

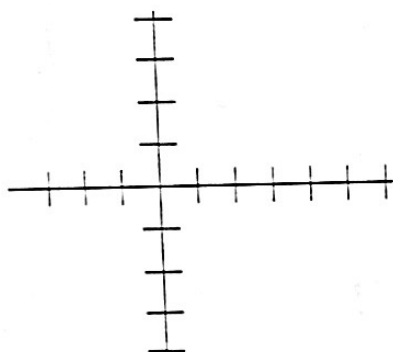
Period: 2π
 Amplitude: 1
 Reflection: None
 Phase Shift: Right $\pi/4$
 Vertical Shift: up 2
 Transformations: _____

Vertical shift up 2
 Horizontal shift right $\pi/4$



17. $y = 3 \cos 2x - 1$

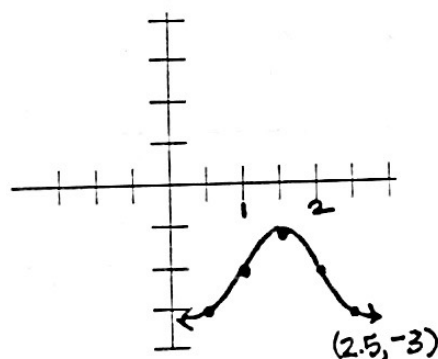
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



18. $y = -\cos \pi x - 2$

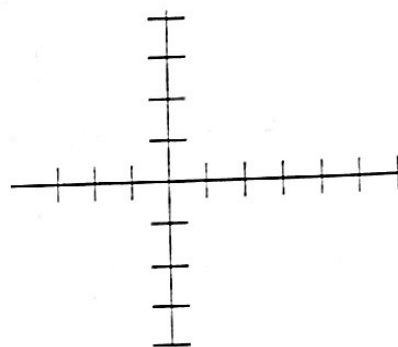
Period: 2
 Amplitude: 1
 Reflection: over y = -2
 Phase Shift: None
 Vertical Shift: down 2
 Transformations: _____

Reflection
 horizontal compression
 vertical shift down 2



19. $y = -\cos(x - \pi) - 1$

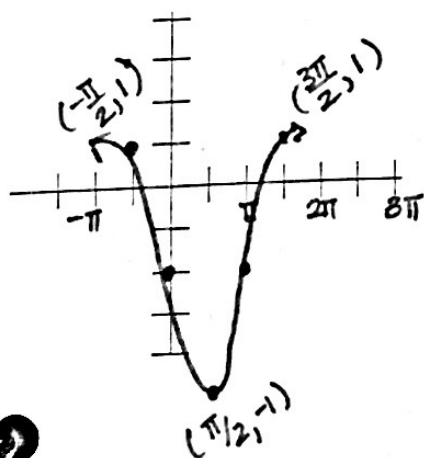
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



20. $y = 3 \cos(x + \frac{\pi}{2}) - 2$

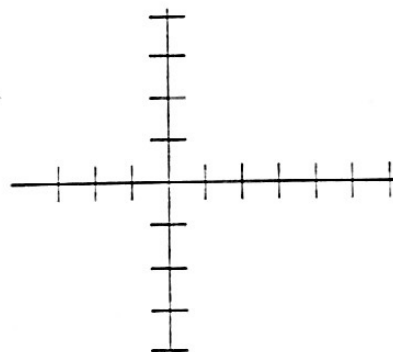
Period: 2π
 Amplitude: 3
 Reflection: None
 Phase Shift: left $\pi/2$
 Vertical Shift: down 2
 Transformations: _____

vertical stretch, horizontal
 shift left $\pi/2$, vertical
 shift down 2 units



21. $y = -2 \cos 2(x - \pi) + 1$

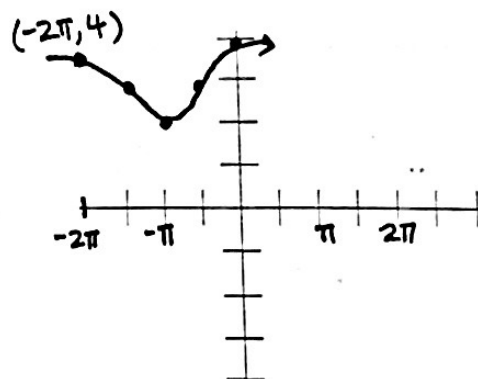
Period: _____
 Amplitude: _____
 Reflection: _____
 Phase Shift: _____
 Vertical Shift: _____
 Transformations: _____



22. $y = \cos(x + 2\pi) + 3$

Period: 2π
 Amplitude: 1
 Reflection: none
 Phase Shift: left 2π
 Vertical Shift: up 3
 Transformations: _____

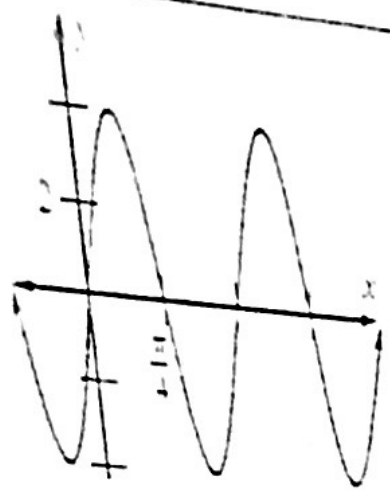
horizontal shift left
 2π units, vertical
 shift up 3



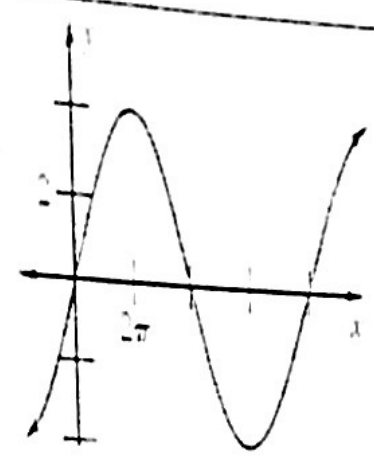
Match the graph with its equation by writing the appropriate letter next to the equation.

A

A.

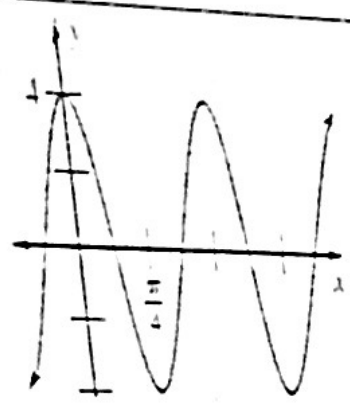


B.

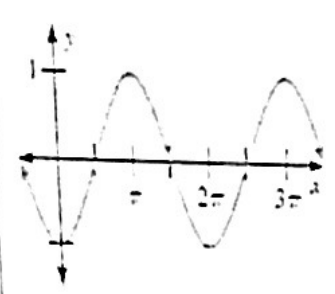


$y = \cos(x - \pi)$ D

C.



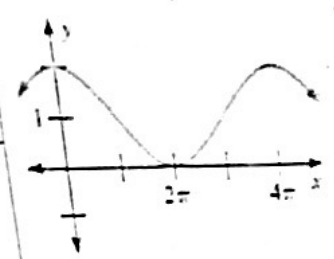
D.



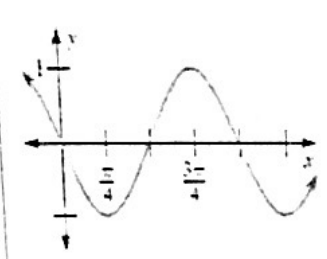
$y = 4 \cos 4x$ C

$y = 4 \sin \frac{1}{4} x$ B

E.



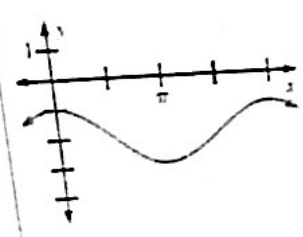
F.



$y = \sin 2\left(x + \frac{\pi}{2}\right)$ F

$y = \cos x - 2$ G

G.



$y = \cos \frac{1}{2} x + 1$ E